

Package: GulFM (via r-universe)

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Type Package

Title General Unilateral Load Estimator for Two-Layer Latent Factor Models

Version 0.5.0

Description Implements general unilateral loading estimator for two-layer latent factor models with smooth, element-wise factor transformations. We provide data simulation, loading estimation, finite-sample error bounds, and diagnostic tools for zero-mean and sub-Gaussian assumptions. A unified interface is given for evaluating estimation accuracy and cosine similarity. The philosophy of the package is described in Guo G. (2026) <[doi:10.1016/j.apm.2025.116280](https://doi.org/10.1016/j.apm.2025.116280)>.

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Suggests testthat (>= 3.0.0), ggplot2

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estimate_gul_loadings *General unilateral load Estimator*

Description

General unilateral load Estimator

Usage

```
estimate_gul_loadings(X, m)
```

Arguments

X	n * p data matrix (already centred and scaled if desired).
m	number of latent factors (both layers).

Details

Step 1: PCA on X to get hat_A1 Step 2: Regress X on hat_A1 to get hat_gF1 Step 3: PCA on hat_gF1 to get hat_A2 Step 4: hat_Ag = hat_A1

Value

A list with hat_A1 : p * m 1st-layer loadings hat_A2 : m * m 2nd-layer loadings hat_Ag : p * m overall loadings Sigma1 : p * p sample cov(X) (for diagnostics) Sigma2 : m * m sample cov(hat_gF1) hat_gF1 : n * m estimated transformed latent factors eig1 : eigen-values of Sigma1 eig2 : eigen-values of Sigma2

Examples

```
dat <- generate_gfm_data(500, 50, 5, tanh, seed = 1)
est <- estimate_gul_loadings(dat$X, m = 5)
err <- sqrt(mean((est$hat_Ag - dat$Ag)^2)) # overall RMSE
```

g_fun	<i>Smooth link functions compliant with Theorems 9&10</i>
-------	---

Description

Returns a vectorised map $g(\cdot)$ and its exact Lipschitz constant L_g for three increasingly nonlinear choices.

Usage

```
g_fun(type = c("linear", "weak_nonlinear", "strong_nonlinear"))
```

Arguments

type Character string selecting the map: "linear", "weak_nonlinear", or "strong_nonlinear".

Value

Named list with components

g_fun	vectorised function $g(\cdot)$
L_g	scalar Lipschitz constant of g

Examples

```
## pick a link with L_g = 1
tmp <- g_fun("linear")
dat <- generate_gfm_data(n = 500, p = 200, m = 5, g_fun = tmp$g_fun)
est <- estimate_gul_loadings(dat$X, m = 5)
err <- norm(est$hat_Ag - dat$Ag, "F")
sprintf("F-error (L_g = %d) = %.3f", tmp$L_g, err)
```

g_theorem	<i>Simulation wrapper for Theorems 9 & 10</i>
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Description

One Monte-Carlo replicate; returns empirical error, exceedance indicator, theoretical bounds, and assumption-check flags.

Usage

```
g_theorem(n, p, m, g_type, epsilon, zero_tol = 0.02)
```

Arguments

n	sample size
p	number of observed variables
m	number of latent factors
g_type	character: "linear", "weak_nonlinear", "strong_nonlinear"
epsilon	error threshold
zero_tol	zero-mean tolerance (default 0.02)

Value

one-row data-frame

Examples

```
df <- g_theorem(500, 200, 5, "linear", 0.6)
```

generate_gfm_data	<i>Generate general factor model with smooth latent transformation</i>
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Description

Generate general factor model with smooth latent transformation

Usage

```
generate_gfm_data(n, p, m, g_fun, seed = 1, sigma_V = 0.1)
```

Arguments

n	Integer: sample size.
p	Integer: number of observed variables.
m	Integer: number of latent factors (both layers).
g_fun	Function: smooth, element-wise transformation applied to latent factors. Must be vectorised, e.g. 'sin', 'tanh', 'scale'.
seed	1.
sigma_V	Numeric: standard deviation of the idiosyncratic noise (default 0.1 => Var = 0.01).

Value

List with components X : n * p matrix of standardised observations. A1 : p * m first-layer loading matrix. A2 : m * m second-layer loading matrix. Ag : p * m overall loading matrix (Ag = A1 F1 : n * m latent factors (before transformation). gF1: n * m latent factors (after transformation). V1 : n * p noise matrix (for diagnostics).

Examples

```
dat <- generate_gfm_data(200, 50, 5, g_fun = tanh)
```

gul_simulation	<i>Single-replication GUL simulation</i>
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Description

Generates one synthetic data set, estimates loadings with the GUL, and evaluates estimation accuracy.

Usage

```
gul_simulation(n, p, m, g_fun)
```

Arguments

n	Integer: sample size.
p	Integer: number of observed variables.
m	Integer: number of latent factors (both layers).
g_fun	Function: element-wise, smooth transformation applied to the latent factors (e.g. 'tanh', 'sin').

Value

Named numeric vector with components error_F : Frobenius norm $\|\hat{A}_g - A_g\|_F$

Examples

```
gul_simulation(200, 50, 5, g_fun = tanh)
```

loading_metrics	<i>Multi-metric evaluation of factor loading matrix estimation error</i>
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Description

Multi-metric evaluation of factor loading matrix estimation error

Usage

```
loading_metrics(A_true, A_hat)
```

Arguments

A_true	True loading matrix (p x m)
A_hat	Estimated loading matrix (p x m)

Value

data.frame with MSE, RMSE, MAE, MaxDev, and Cosine similarity

Examples

```
## simulated example
p <- 100; m <- 5
Ag_true <- matrix(rnorm(p*m), p, m)
Ag_hat <- Ag_true + matrix(rnorm(p*m, 0, 0.1), p, m)
metrics <- loading_metrics(Ag_true, Ag_hat)
print(metrics)
```

verify_mean

Verify zero-mean preservation (Theorem 10 assumption 2a)

Description

Draws n i.i.d. $N(0, I_m)$ latent factors, applies g component-wise, and checks whether $|E[g(x)]| < \text{tol}$ on every coordinate.

Usage

```
verify_mean(g_fun, m = 5, n = 10000, tol = 0.001)
```

Arguments

<code>g_fun</code>	vectorised map $g: \mathbb{R} \rightarrow \mathbb{R}$
<code>m</code>	latent dimension
<code>n</code>	Monte-Carlo sample size
<code>tol</code>	numerical tolerance (default $1e-3$)

Value

logical TRUE if $|\text{lmean}| < \text{tol}$ on all coords

Examples

```
tmp <- g_fun("weak_nonlinear")
verify_mean(tmp$g_fun, m = 5)
```

verify_subgaussian *Verify sub-Gaussian preservation*

Description

Draws n i.i.d. $N(0, I_m)$ latent factors, applies g component-wise, and checks whether $E[\exp(g(x))]$ remains below an empirical cut-off. This is a quick proxy for finite sub-Gaussian norm.

Usage

```
verify_subgaussian(g_fun, m = 5, n = 1000, cut = exp(2))
```

Arguments

<code>g_fun</code>	vectorised map $g: \mathbb{R} \rightarrow \mathbb{R}$
<code>m</code>	latent dimension
<code>n</code>	Monte-Carlo sample size
<code>cut</code>	empirical threshold (default $\exp(2)$ & 7.389)

Value

logical TRUE if $E[\exp(g)] < \text{cut}$ on all coords

Examples

```
tmp <- g_fun("strong_nonlinear")
verify_subgaussian(tmp$g_fun, m = 5)
```

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